

An encounter with Petr Vopěnka

Kateřina Trlifajová

katerina.trlifajova@fit.cvut.cz

Tribute to Kurt Gödel

Brno, January 13 - 15, 2020



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- ▶ Childhood in Dolní Kralovice.
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- ▶ Doctor of Sciences 1967.
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- ▶ Professorship was prepared in 1968.
- ▶ Vice-Dean 1966 - 1969.
- ▶ Russian occupation of Czechoslovakia in 1968.
- ▶ Employee in a subsidiary position, 1970 - 1989.

Dolní Kralovice



Kralovická pouť 1953

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- ▶ Died on 29th March 2015. The day of a solar eclipse.

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- ▶ Set-theoretical seminar (B. Balcar, L. Bukovský, P. Hájek, K. Hrbáček, T. Jech, A. Sochor, P. Štěpánek, and others).
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- ▶ Theoretical cybernetics. (M. Chytil, R. Kryl, P. Pudlák, P. Vojtáš...)

Vopěnka's set-theoretical seminar in 1998



B. Balcar, P. Štěpánek, P. Hájek, P. Vopěnka, A. Sochor, L.
Bukovský

D. Harmancová, P. Jechová, K. Bendová, A. Sochorová, T. Jech

Alternative Set Theory

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- ▶ Petr Hájek, Petr Vopěnka, *Theory of Semisets*, North-Holland Publishing Company, 1972.

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- ▶ Alternative Set Theory. (K. Čuda, J. Miček, A. Sochor, A. Vencovská, P. Zlatoš, and others)

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- ▶ Pilsen seminar (M. Holeček, M. Větrovcová, J. Romportl)
- ▶ *Prolegomena*, Karolinum, Praha 2014.
- ▶ *New Infinitary Mathematics I. - IV.*, Karolinum, Praha 2016.

History of Mathematics

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- ▶ Geometry.

Four *Discourses with Geometry*, 1989 - 1995.

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Relation of the surface and the volume of a sphere
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Proof of God's existence. (Kurt Gödel)

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How to Measure the Infinite. Mathematics with Infinite and Infinitesimal Number, World Scientific, 2019.

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Return to phenomena themselves.

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- ▶ **Horizon.** An indistinct limit separating the field of direct experience from indirect experience.

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Meditations on Foundations of Science, Práh, 2001.

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Phenomenological interpretation of infinity and continuum.

Meditations on Foundations of Science



“The second more meaningful phenomenon immediately after the horizon, which modern science has denied a place in the subject of its study, is the phenomenon of indiscernibility. We show that through this phenomenon we interpret the phenomenon of continuity and that the cohesiveness of the world is actually based on this phenomenon, interpreted as a collection of objects.”

Philosophical Seminar

Summer Philosophical School in Sázava 2001 - 2011 (P. and K.Floss, Z.Neubauer, I.M.Havel, J.Fiala, M.Větrovcová, M.Holeček, P. Zamarovský)

